

Applications with the Newest Multi-spectral Environmental Satellites

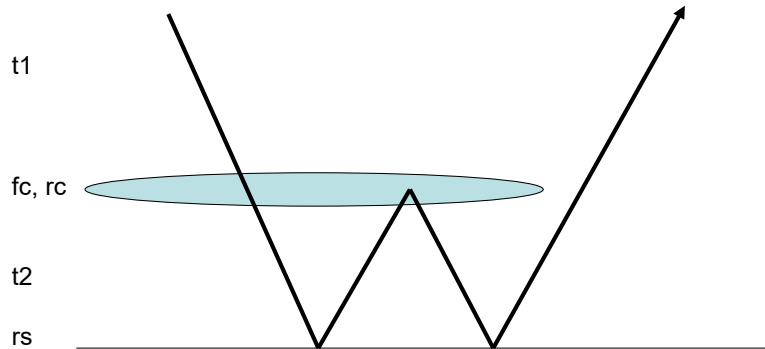
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3-13 June 2007

Homework Assignment (Due 11 June 2007)

1. What is the ratio of blackbody radiances at $B(10 \mu\text{m}, 300 \text{ K})$ and $B(0.5 \mu\text{m}, 6000 \text{ K})$? Estimate this without calculating the radiances explicitly.
2. If the $4 \mu\text{m}$ brightness temperature is 310 K and the $11 \mu\text{m}$ brightness temperature is 290 K , what fraction of the radiance at $4 \mu\text{m}$ is due to reflected solar radiation? Use the fact that $B(4 \mu\text{m}, T)$ is proportional to T^x where $x \sim 12$.
3. If the effective temperature of Earth is 255 K (defined as blackbody temperature at which solar energy received is equal to infrared energy released) and the surface temperature is 285 K , what is the average absorptance of the atmosphere of Earth to infrared radiation? Assume that the surface behaves like a blackbody and the atmosphere is transparent to solar radiation; use conservation of energy at the top of the atmosphere and at the surface to derive your answer.
4. Measurements of outgoing radiation from the earth-atmosphere system in a nadir viewing radiometer yield brightness temperatures of 310 K in the infrared window at 900 cm^{-1} , 220 K in the CO_2 band at 660 cm^{-1} , and 280 K in the O_3 band at 1040 cm^{-1} . What is the transmission of the ozone layer at 1040 cm^{-1} ? Assume the earth surface radiates as a blackbody, the stratosphere is opaque at 660 cm^{-1} , and the ozone resides exclusively in the stratosphere. Note that Planck radiances $B(1040 \text{ cm}^{-1}, T) = 14.8, 64.1,$ and $107.9 \text{ mW/m}^2/\text{ster/cm}^{-1}$ for $T = 220 \text{ K}, 280 \text{ K},$ and 310 K respectively.
5. Two window channels (11 and $12 \mu\text{m}$) are viewing the ocean in cloud free conditions. The observed brightness temperatures are 297 K and 294 K . The respective atmospheric transmittances are $.98$ and $.95$. (a) What is the ratio of the absorbing powers k_{w11}/k_{w12} ? (b) What is the SST?
- 6a. The ocean surface at 300 K is covered by a layer of water vapor at 280 K with an optical depth of 0.05 in the infrared window (IRW) at 11 microns. The MODIS IRW measurement will be less than 300 K due to atmospheric water vapor absorption; what correction must be made to the measured brightness temperature to arrive at the correct SST? Assume the ocean surface behaves like a blackbody, express the transmittance of the water vapor $\tau = 1 - \sigma$, and use the fact that at 11 microns the Planck radiance is proportional to T^4 .
- 6b. If the earth surface is not a blackbody but has an emissivity of 0.9 , what is your answer?

7. A model atmosphere consists of an upper layer with transmittance t_1 , a partial cloud layer with fractional area f_c covered by clouds with reflectance r_c in either direction, and a lower layer with transmittance t_2 . The earth surface has an average reflectance r_s . (a) Ignoring scattering in the layers and absorption in the clouds, derive an expression for F , the fraction of solar radiation making it out of earth-atmosphere via the indicated path. (b) If t_2 decreases by 1% (due to low level pollution), what is the corresponding percentage change in F ?



8. Consider an atmosphere where the temperature profile is given by $T(p) = 200 + 100(p/ps)$ in degrees K. The transmittance for a microwave spectral band is given by $\tau(p) = 1.0 - 0.7(p/ps)$. Assuming reflection is negligible at the earth surface, what is the brightness temperature observed by the microwave sensor in this spectral band? Start with the RTE to develop your answer.